

Review Article

Statistical methods in the meta-analysis of prevalence of human diseases

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ABSTRACT

**Background & Aim:** A meta-analysis refers to the statistical synthesis of results from a series of studies and has been used to estimate pooled prevalence of human diseases. In this study, we review some statistical issues regarding the meta-analysis of the prevalence of human diseases such as statistical software and programs, transformations of prevalence rate, assessment of heterogeneity, and publication bias.

Introduction

A meta-analysis refers to the statistical synthesis of results from a series of studies. If an effect size is consistent across the series of studies, the meta-analysis procedures can be used to report that the effect is robust across the samples and to estimate the magnitude of the effect more precisely than we could obtain in any of the individual studies (1). The prevalence is defined as the number of persons with a health event of interest (e.g., disease) present in the population at a specific time divided by the total number of persons in the population at that time (2). Prevalence is a proportion, which can be

categorized as point prevalence (total number of existing health events in a population at a given time point) and period prevalence (total number of existing health events in a population during a specified time period). Several software and programs have been used in the estimation of the pooled prevalence of human diseases. For example, the comprehensive meta-analysis software (Biostat, Englewood, NJ, USA, [www.Meta-analysis.com](http://www.Meta-analysis.com)) has been used to estimate the pooled prevalences of depressive symptoms in patients with chronic obstructive pulmonary disease (3), and HIV among high school and college student in China (4). Furthermore, Chen et al. (5) determined the prevalence of coinfection with either hepatitis C virus or hepatitis B virus in patients infected with HIV and Jayawardena et al. (6) discussed the prevalence of pre-diabetes and diabetes in South Asia using the Review Manager (RevMan

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computer program, Cochrane Collaboration, London, UK, [www.cc-ims.net/RevMan](http://www.cc-ims.net/RevMan)). Mitchell et al. (7) summarized the pooled prevalence of depression, anxiety, and adjustments disorders and Luppá et al. (8) analyzed the age- and gender-specific prevalence of depression in latest-life using the statistical package StatsDirect (StatsDirect Ltd., England, [www.statsdirect.com](http://www.statsdirect.com)). The MetaXL is a new, freely available, software program for the meta-analysis in Microsoft Excel (Australia, [www.epigear.com](http://www.epigear.com)) and has been used to estimate the multiple category prevalence of multiple sclerosis (9). General purpose statistical package, such as SAS, SPSS, and STATA, has no inherent support for meta-analysis. However, some macros have been developed to perform meta-analysis of prevalence. For example, several studies have used the STATA statistical software package (StataCorp LP, College Station, Texas, USA) (5, 10-12), a general mixed effects linear models approach using SAS (PROC GLIMMIX macro for SAS, Cary NC, USA) (13, 14), and macros using SPSS software (SPSS, Inc., Chicago, IL, USA) (15, 16). Furthermore, some studies conducted Bayesian logistic meta-regression with the help of WINBUGS software (WinBUGS software, MRC Biostatistics Unit, Cambridge, UK) (17, 18). The basic features and similarities and differences among these software and programs can be found in the book "Introduction to Meta-Analysis" by Borenstein and Hedges (1) and the website: [www.Meta-analysis.com](http://www.Meta-analysis.com).

### Pooled Prevalence of Human Diseases

The prevalence has two features: (1) it is always between 0 and 1 (inclusive) and (2) the sum over categories always equals 1. Therefore, it is assumed that prevalence follows a binomial distribution (9). The pooled prevalence is an average of the individual study results weighted by the inverse of their variances using a fixed/random effects model (19).

According to Barendregt et al. (9), the variance of prevalence can be expressed as  $\text{Var}(p) = p(1-p)/N$ , where  $p$  is the prevalence proportion, and  $N$  is the population size. Then, the

pooled prevalence can be expressed as follows:

$$p = \frac{\sum_i \frac{p_i}{\text{Var}(p_i)}}{\sum_i \frac{1}{\text{Var}(p_i)}}$$

With standard error (SE),

$$\text{SE}(p) = \sqrt{\sum_i \frac{1}{\text{Var}(p_i)}}$$

The confident interval of the pooled prevalence can be expressed as follows:

$$\text{CI}_\gamma(p) = P \pm Z_{\alpha/2} \text{SE}(p)$$

Where,  $Z_{\alpha/2}$  is the appropriate factor from the standard normal distribution for the desired confidence percentage (e.g.,  $Z_{0.025} = 1.96$ ).

The inverse variance method works fine for the prevalence proportions around 0.5. However, it arise problems when the proportions get closer to 0 or 1. For example, when the proportion becomes small or big, the variance of the study is squeezed toward 0. To normalize the distribution of the effect size, the natural logarithm (log) of prevalence has been used to estimate the pooled prevalence (3, 20) with the variance-based method (19). After the meta-analysis, the effect sizes should be converted back into prevalence (3). However, the commonly used logit transformation cannot succeed in stabilizing the variance. Barendregt et al. (9) proposed that the double arcsine transformation is preferred over the logit transformation, and the method is also suitable to meta-analysis of multiple category prevalence.

### Assessment of heterogeneity

The pooled prevalence estimates and 95% confidence intervals, stratified by study setting and other covariates, can be determined by fixed/random effects meta-analysis using the inverse variance method (19) based on the heterogeneity test result that can be assessed using Cochran's Q statistics,  $I^2$  (21), and  $\tau^2$  statistics (22). The Q statistic is reported with  $\chi^2$  and P values. For Q statistics, due to the low power of this test, a minimum cut-off P value of 0.10 has been established as a threshold of heterogeneity (4, 10, 21, 23).  $I^2$  lies between 0% and 100% and  $\tau^2$  show the variance between studies. The  $I^2$  statistic is reported as a

percentage with increasing values indicating greater heterogeneity between estimates of individual studies. For example, the general interpretation of  $I^2$  values is: 0-40% might indicate low heterogeneity, 30-60% may represent moderate heterogeneity, 50-90% may represent substantial heterogeneity, and 75-100% may indicate considerable heterogeneity (Cochrane Handbook for Systematic Reviews of Interventions. <http://www.cochrane-handbook.org>) (24). Several studies have used  $I^2$  to assess heterogeneity with thresholds of  $\geq 25\%$ ,  $\geq 50\%$  and  $\geq 75\%$  indicating low, moderate and high heterogeneity, respectively (3, 4, 12, 23, 25).

In the fixed effects model, it is assumed that all of the observed differences between studies are due to chance, where the inverse variance is used for the weighted method. A random effects model is recommended for the meta-analysis of prevalence when heterogeneity is observed in prevalence estimates across studies (19) as a fixed effects model is likely to produce misleading results in the presence of significant heterogeneity (26). For the random effects model, it is assumed that each study may have a different underlying effect. This model leads to relatively more weight being given to smaller studies and to wider confidence intervals than the fixed effects models.

We can also test the heterogeneity by conducting a meta-regression analysis. Meta-regression can be used to estimate the extent to which measured covariates could explain the observed heterogeneity in prevalence estimates across studies. The regression coefficients ( $\beta$ ) indicate the average difference in prevalence proportion for one category compared to the other. Effects of individual covariates can be examined first in univariate models and then in a multivariate model constructed in a step-wise fashion. When evidence is found of heterogeneity in the prevalence estimates between studies, meta-regression with Z-test can be used to identify moderators which might contribute to the heterogeneity of prevalence (27-30).

The source of heterogeneity can be the differences due to inadequate sample size, different study design, different populations, different treatment, different adjustments,

different statistical analyses, different reporting, etc. To deal with the statistical heterogeneity, following analyses can be conducted such as do subgroup analysis (such as sex, age, and geographical design), exclude the outlying studies, choose another scale or change the effect measure, perform random effects meta-analysis, and meta-regression (4, 5, 11, 24, 30).

### **Assessment of publication bias**

In meta-analysis, the publication bias can be checked using the Begg's funnel plot (5, 10, 12, 31). If publication bias is not present, the funnel plot is expected to be roughly symmetrical. The publication bias can be further checked using three statistical tests. First, the Egger test is a test for asymmetry of the funnel plot (32). This test is based on a linear regression of normalized effect estimate (estimate divided by its SE) against precision (reciprocal of the SE of the estimate). The intercept provides a measure of asymmetry – the larger its deviation from zero, the more pronounced the asymmetry (5, 7, 10, 12). Second, the Harbord's test (33) is similar to Egger's test but uses a modified linear regression method to reduce the false positive rate, which is a problem with the Egger test when there are a large treatment effects, few events per trial or all trials are of similar sizes (8, 10). Third, the Begg and Mazumdar's test (34) tests the interdependence of variance and effect size using rank correlation method (4, 7, 10, 12). In general, the significance is set at a  $P \leq 0.05$  (4, 11). However, some authors have suggested that the recommended level is a  $P \leq 0.10$  for the test of publication bias (5, 20, 35).

### **Conclusion**

The meta-analysis is a useful tool to estimate the pooled prevalence of human diseases. The double arcsine transformation of single and multi-category prevalence is preferred over the commonly used logit transformation when the prevalence is small or large, with the consequence that such studies get a large weight in the meta-analysis. The Bayesian approach may have some advantages because it can take

into account all sources of variations and reflect these variations in the pooled result. When heterogeneity is observed, several methods can be used to do further analyses such as performing subgroup analysis, excluding the outlying studies, and conducting random effects analysis and meta-regression. Studies with small sample size may cause bias. It is suggested that some studies with small sample size may be excluded from the meta-analysis when bias is observed by graphic or statistic test method.

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